2D-DOA Estimation of Patch Antenna Array Using USV - MUSIC Algorithm

Vira Rahayu†,‡ Kei Yokokawa† Qiang Chen† and Yono Hadi Pramono‡

† Departement of Communication Engineering, Graduate School Of Engineering Tohoku University 6-6-05 Aoba, Aoba-ku, Sendai, Aramaki, 980-8579 Japan
‡ Physics Department, Faculty of Mathematical and Science, Institute Teknologi Sepuluh Nopember Jl. Arief Rahman Hakim, Sukolilo, Surabaya, 60111 Indonesia
E-mail: †{vira, yokokawa, chenq}@ecei.tohoku.ac.jp, ‡kajur_fisika@its.ac.id

Abstract Universal steering vector (USV) is applied to estimate directional of arrival (DOA) using multiple signal classification (MUSIC) algorithm. The USV that includes effect of mutual coupling can be used in searching peak spectrum directly without compensation of the mutual coupling. The circular patch antenna is used as DOA receiving antenna for estimation of DOA. Comparison between results of the CSV (conventional steering vector) and the USV are presented in this research.

Keywords Direction of arrival, MUSIC, mutual coupling, steering vector, antenna

1. Introduction

Direction of arrival estimation becomes one of the most important parts of smart antennas application. There are many algorithm can be used to estimate direction of arrival such as: MUSIC, Root-MUSIC, ESPRIT, etc [1][2][3][4]. Multiple signal clarification is one of effective algorithms to estimate DOA. The original approaches of MUSIC algorithm do not include mutual coupling effect of array antenna. But in practical conditions, effect of mutual coupling can not be ignored. There are many researchers who have studied the problem to reduce the effect of mutual coupling from received voltage at the array terminal or from the steering vector and then apply compensated received voltage or compensated steering vector to evaluate the MUSIC spectrum[3][5][6][7].

Many studies have been focused on the methods to compensate effect of mutual coupling on array antenna. Studies about the mutual coupling effect using a circuit theory approach have been done[8]. More recently, researchers tried to analyze the mutual coupling using the electromagnetic interaction approach and calibration method. But the compensated method in [8] can not be generally used. This method is only valid and accurate for small dipole antennas. Studies about effect of mutual coupling are also redefined by talking the open circuit scattering into account, but the problem is the current distribution has to be estimated in advance. Estimation of current distribution will become difficult when the structure of antennas is complicated. This is because current distribution depends on direction and polarization of incident waves.

In the previous researches, effect of mutual coupling that is compensated from steering vector has been studied. It is possible to use the USV to calculate MUSIC spectrum directly without compensation and the steering vectors has been evaluated by using method of moments (MoM) for array antenna with arbitrary geometry[1].

In this report, a circular patch antenna array using USV-MUSIC algorithm is applied to DOA Estimation. The USV is used to calculate MUSIC spectrum of circular patch antenna array. The result will be compared between USV-MUSIC and CSV-MUSIC.

2. DOA Estimation Using MUSIC Algorithm

There are two subspaces that are divided by received signal space of M array elements. The first is incident signal subspace spanned by L incident signal eigenvectors and the other is the noise subspace spanned by M-L noise eigenvector. As many adaptive techniques, MUSIC is dependent on the correlation matrix of the vector of received signals. Both of signal eigenvector and noise eigenvector can be calculated by correlation matrix of received voltage \([V^\top]\) at the terminals of the antenna element as

\[
[R_{xx}] = E([V^\top][V^\top])^H
\]

where \(E()\) denotes the statistical expectation and superscript \(H\) denotes the complex conjugate transform.

The received voltages by array antenna, which is corrupted by noise, is expressed as:
Fig 1. Ten elements patch antenna array

Figure 2. MUSIC DOA estimation of ten elements patch antenna circular array with the CSV

Figure 3. MUSIC DOA estimation of ten elements patch antenna circular array with the USV

Table 1. MUSIC Spectrum of the CSV and the USV

<table>
<thead>
<tr>
<th>Angle</th>
<th>CSV</th>
<th>USV</th>
</tr>
</thead>
<tbody>
<tr>
<td>60°,70°</td>
<td>131.9</td>
<td>78.94</td>
</tr>
<tr>
<td>60°,40°</td>
<td>136.4</td>
<td>64.62</td>
</tr>
<tr>
<td>80°,40°</td>
<td>127.1</td>
<td>49.51</td>
</tr>
<tr>
<td>30°,50°</td>
<td>128.7</td>
<td>29.12*</td>
</tr>
<tr>
<td>20°,10°</td>
<td>125.2</td>
<td>72.43</td>
</tr>
<tr>
<td>110°,20°</td>
<td>129.8</td>
<td>31.19</td>
</tr>
<tr>
<td>110°,50°</td>
<td>128.9</td>
<td>21.42*</td>
</tr>
</tbody>
</table>

*error at [30,50] become [29,47] and at [110,50] become [116,58]

\[
[V^r] = \sum_{m=1}^{L} [A(\theta_m, \phi_m)]s(\theta_m, \phi_m) + \text{Noise} \tag{2}
\]

where \([A]\) represents steering vector that have \(M\) dimension. \(s(\theta_m, \phi_m)\) denotes the electric field of \(m\)th incident wave.

MUSIC direction of arrival estimation utilizes orthogonality between the signal eigenvector and the noise eigenvector. DOA estimation can be done by searching peak of the MUSIC spectrum that given by:

\[
P_{\text{MUSIC}}(\theta, \phi) = \frac{[A(\theta, \phi)]^H[A(\theta, \phi)]}{[A(\theta, \phi)]^H[E_s][E_s]^H[A(\theta, \phi)]} \tag{3}
\]

\(\theta\) and \(\phi\) are searching angles, and the polarization of the incident wave is assumed to be known. \([A]\) represents the CSV and \([E_s]\) is the signal eigenvector that have size \(M \times (M-L)\) matrix whose columns are the \(M\) noise eigenvectors of matrix correlation.

In this report, the USV is used which includes effect of mutual coupling between antenna elements. MUSIC spectrum by using the USV given by:

\[
P_{\text{MUSIC}}(\theta, \phi) = \frac{[A^u(\theta, \phi)]^H[A^u(\theta, \phi)]}{[A^u(\theta, \phi)]^H[E_s][E_s]^H[A^u(\theta, \phi)]} \tag{4}
\]

The spectrum is compared with that defined in eq. (3) of the CSV.

3. Conventional Steering Vector

3.1. Conventional Steering Vector

The received voltage vector with \(M\) dimensions and \(L\) incident waves are defined by
\[ [V] = \sum_{m=1}^{i} [A(\theta_m, \phi_m)] f(\theta_m, \phi_m) s(\theta_m, \phi_m) + \text{Noise} \quad (5) \]

where \( f(\theta_m, \phi_m) \) represents ideal isolated element pattern that is the same at all elements. \([A(\theta_m, \phi_m)]\) is the CSV that have \( M \) dimension. \( m \)th element of \([A(\theta_m, \phi_m)]\) is defined by

\[ a_i(\theta_m, \phi_m) = e^{jK_m (r_i - r_0)} \quad (6) \]

3.2. Universal Steering Vector

The USV is evaluated using method of moments to get accuracy estimation. Each patch antenna is divided into several segments. Richmond’s method give the rule that the length of segment must be less than \( \lambda/2\pi \). The matrix for unknown current of all segments given by

\[ [Z][I] = [V^{inc}(\theta, \phi)] \quad (7) \]

where \([Z]\) is matrix or impedance whose element \( z_{ij} \) that represents mutual impedance between \( i \)th and \( j \)th segment. \([Z]\) has size \( N \times N \) impedance matrix is obtained by full wave analysis that become independent of the incident wave. \([I]\) is the matrix of current that represents the current of all segments. This matrix have \( N \) size. \( N \) voltage represent the inner product of the weighting function and the incident electrics from direction \((\theta, \phi)\) for all segments. The unknown current can be obtained by equation

\[ [I] = [Y][V^{inc}(\theta, \phi)] \quad (8) \]

where \([Y]\) is inverse matrix from admittance matrix\([Z]\). Then, current matrix at terminal of antenna can be defined as

\[ [I_{\text{ter}}] = [Y_{\text{ter}}][V^{inc}(\theta, \phi)] \quad (9) \]

where \([I_{\text{ter}}]\) represents the current vector at terminal segment. \([Y_{\text{ter}}]\) is matrix that shows mutual admittances between the segments at terminals and all the segments of array antenna. \([Y_{\text{ter}}]\) is part of \([Y]\) that include mutual coupling effect.

The USV that includes effect of mutual coupling can be shown as follow

\[ [A^\nu(\theta, \phi)] = Z_{\text{t}}[Y_{\text{ter}}][V^{inc}(\theta, \phi)] \quad (10) \]

Assuming the terminal of array is loaded by an impedance of \( Z_t \).

4. Simulation Result

Fig 1. Shows ten elements patch antennas array where each element is loaded by impedance \( Z_t = 50 \, \Omega \). The antenna is rectangular patch antenna that have ground plane. Fig. 2 and Fig 3 show spectrum MUSIC of ten elements patch circular array. All incident waves have signal to noise ratio (SNR) of 20 dB. Because the number of array antenna is 10, 7 DOA can be detected at same time. The DOA with direction are \([60^\circ,70^\circ]\), \([60^\circ,40^\circ]\), \([80^\circ,40^\circ]\), \([30^\circ,50^\circ]\), \([20^\circ,10^\circ]\), \([110^\circ,20^\circ]\) and \([110^\circ,50^\circ]\). All directions of the sources signal can be detected by the USV, it is demonstrated result in all correct DOA, while the CSV can also detect 7 directions but there are including several errors. It can be seen at Table 1.

5. Conclusions

DOA estimation of circular patch antenna array using USV-MUSIC algorithm have been done. The USV was used to calculate MUSIC spectrum of linear patch antenna array. It was demonstrated by the numerical simulation the USV that includes effect of mutual coupling gives more accurate results than the CSV.

6. Acknowledgement

The authors wish to acknowledge the financial support of the JASSO Scholarship.

References


